

# Pascal vs KNL : Performance Evaluation with ICCG Solver

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## Motivation

- Top 10 supercomputers of the Green 500 List use many-core devices
  - ✓ NVIDIA Pascal GPU, Intel Xeon Phi (KNL)
  - ✓ Development of the algorithms and optimization techniques for many-core devices is required.
- To know the characteristics, we evaluated the performance of new many-core devices



Reedbush (ITC, U-Toyo)

- Reedbush-U: CPU (Intel Xeon E5-2695) nodes x420
- Reedbush-H: CPU (Intel Xeon E5-2695) + GPU (NVIDIA Tesla P100) nodes x120

Oakforest-PACS (JCAHPC)

- TOP 500 #6 (#1 in Japan)
- 8,208 Intel Xeon Phi (KNL)
- 25 PF Peak Performance

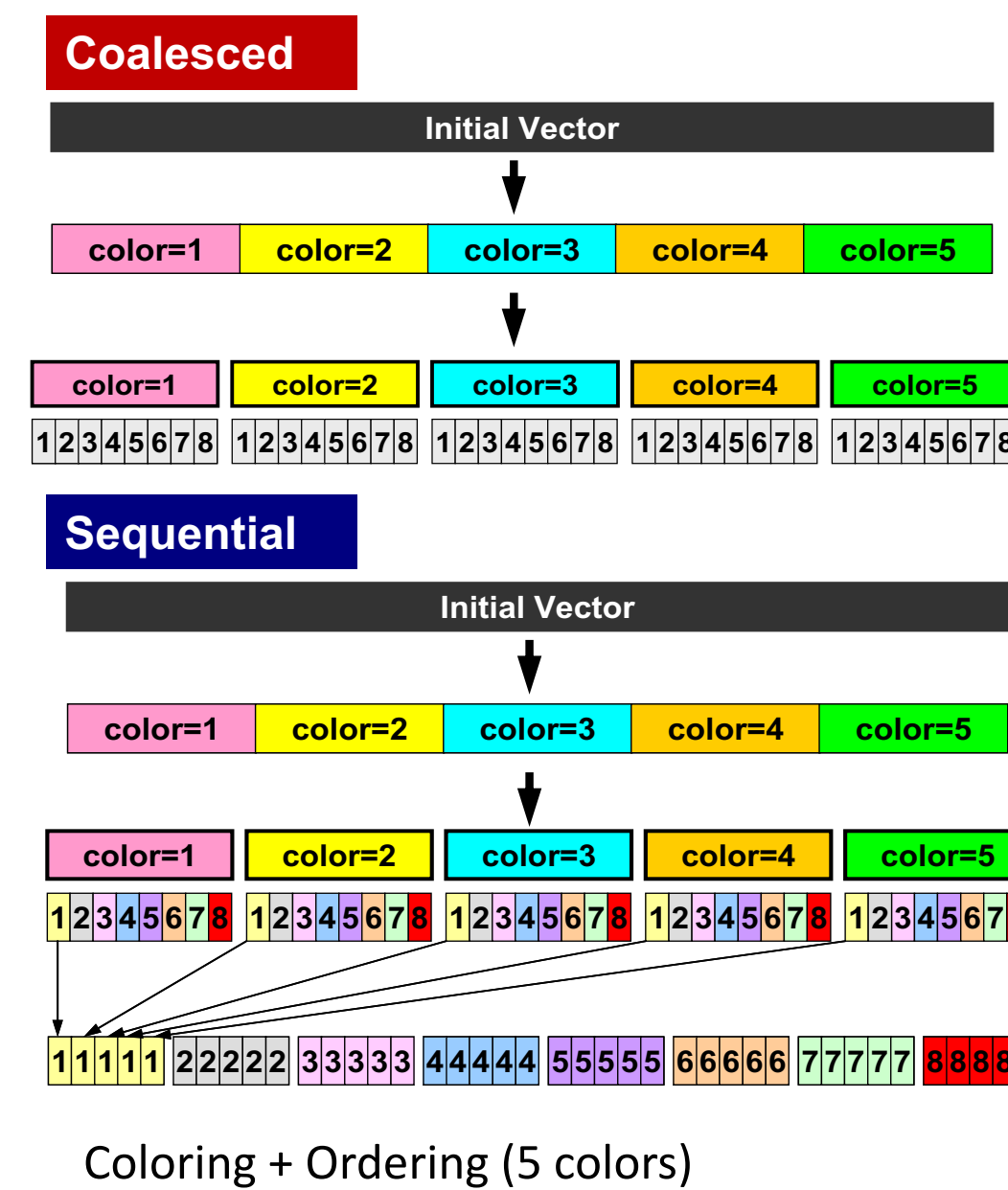
## ICCG Solver

- ICCG: Data Dependency for Incomplete Cholesky Factorization
- Fortran 90 + OpenMP/OpenACC
- Reordering required for parallelization
  - ✓ CM-RCM + Coalesced/Sequential
- Storage of Matrix
  - ✓ CRS, ELL(Ellpack-Itpack), SELL-C- $\sigma$

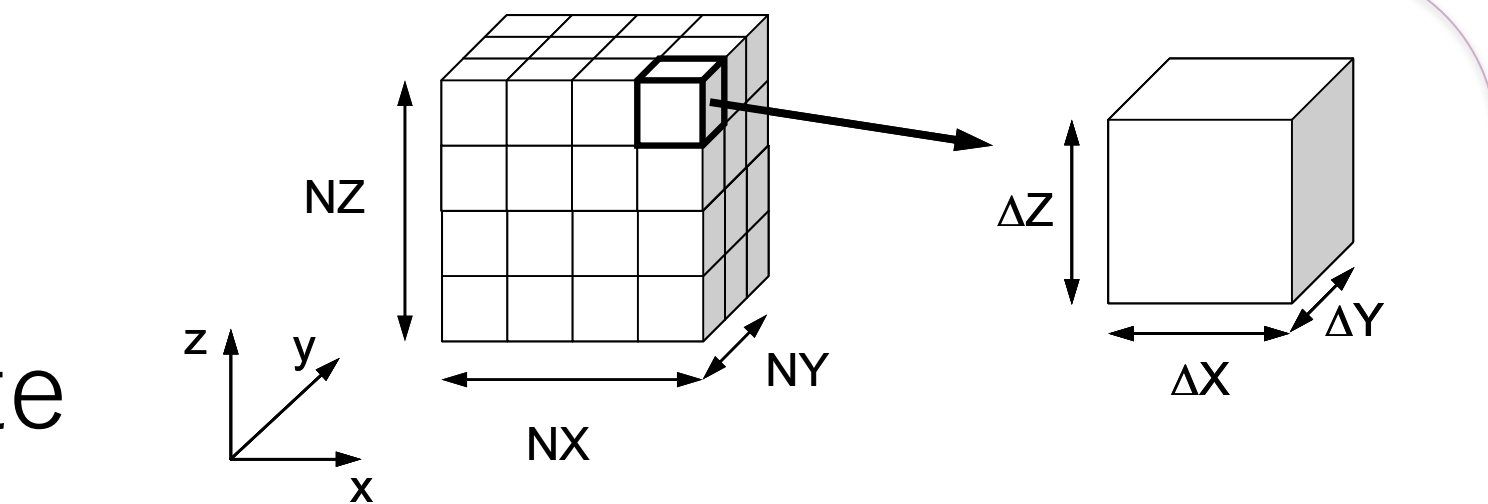
```

Compute r(0) = b - [A]x(0)
for i = 1, 2, ...
  solve [M]z(i-1) = r(i-1)
  pi-1 = r(i-1)z(i-1)
  if i = 1
    p(1) = z(0)
  else
    βi-1 = pi-1/pi-2
    p(i) = z(i-1) + βi-1p(i-1)
  endif
  q(i) = [A]p(i)
  αi = pi-1/p(i)q(i)
  x(i) = x(i-1) + αip(i)
  r(i) = r(i-1) - αiq(i)
  check convergence |r|
end
    
```

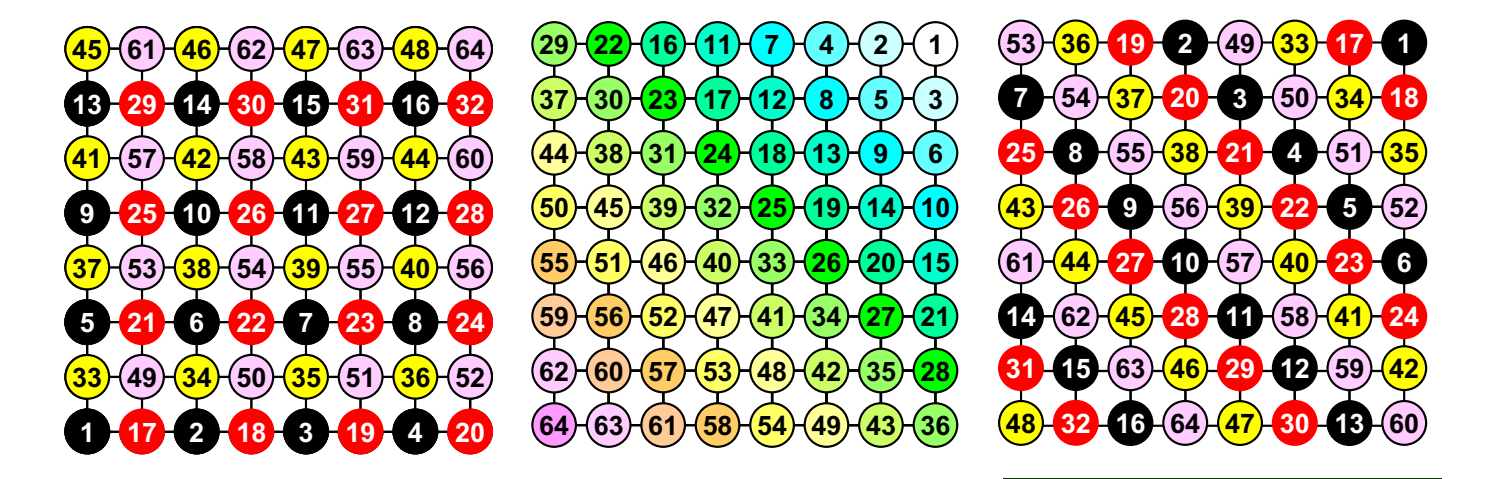
ICCG algorithm.



Coloring + Ordering (5 colors)

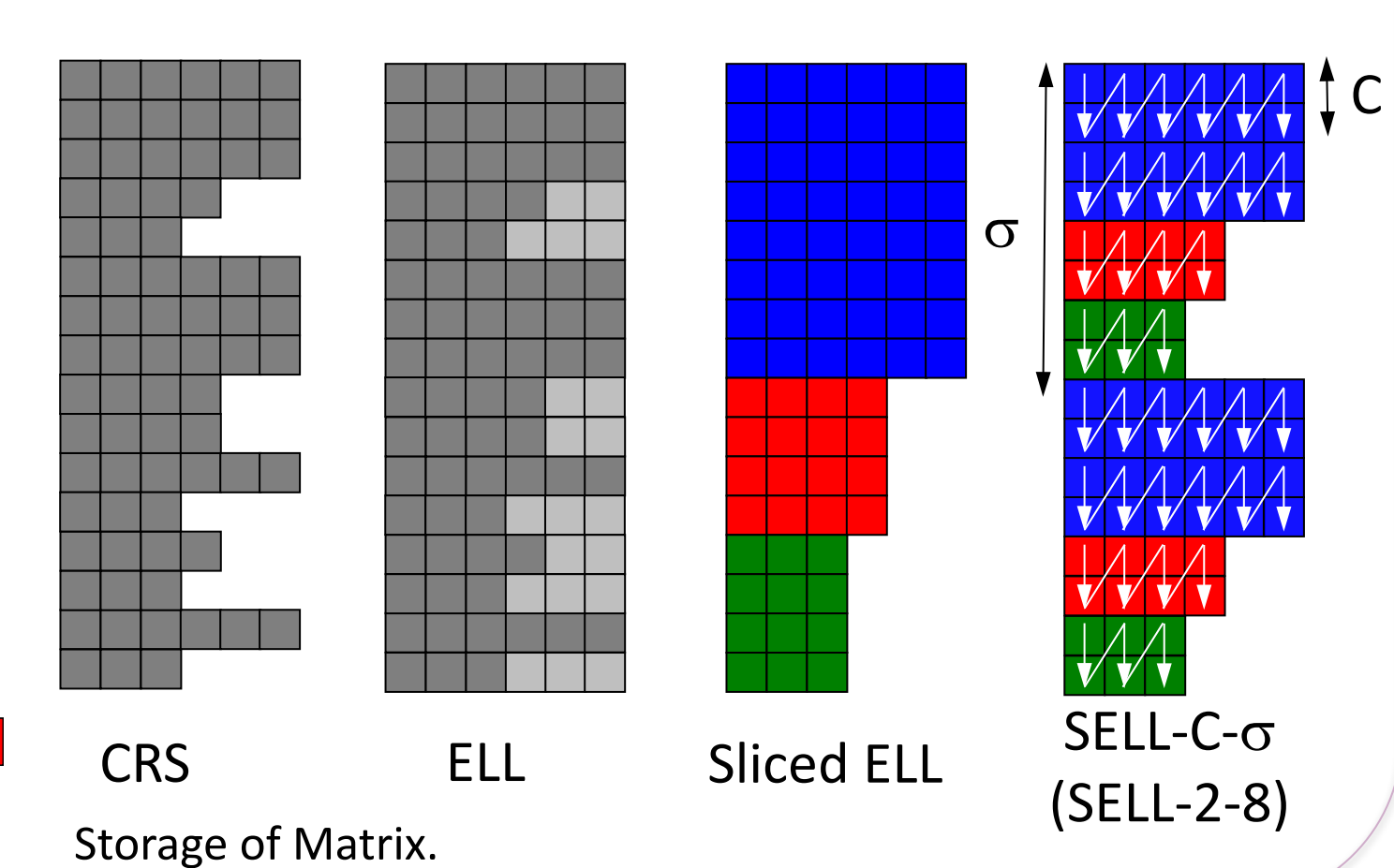


Target App: Finite Volume Method, Poisson Equations (128<sup>3</sup> cells)  
 • FDM-type mesh (7-pt. Stencil), Unstructured data structure  
 • SPD matrix



MC (Color# = 4) Multicoloring  
 RCM Reverse Cuthill-McKee  
 CM-RCM (Color# = 4) Cyclic MC + RCM

Coloring and reordering for parallelization. In this evaluations, we used CM-RCM reordering.



Storage of Matrix.

## Performance Evaluation

- Evaluate with several devices
  - ✓ GPU (Pascal/Kepler), Xeon Phi (KNC/KNL), CPU (Broadwell)
    - KNL: Flat-Quadrant, MCDRAM
  - ✓ Compiler
    - OpenACC: pgfortran 17.1 -acc -O3 -ta=tesla:cc60
    - OpenMP: ifort 17.0.1 -align array64byte -O3 -xMIC-AVX512 -qopenmp -qoptstreaming-stores=always -qopt-streaming-cache-evict=0

- Optimizations for P100
  - Baseline
    - ✓ Insert !\$acc kernels to all loops to be parallelized
  - Async
    - ✓ Attach async(0) clause
  - Thread
    - ✓ Optimize gang/vector parameters
  - Fusion
    - ✓ Kernel fusion to reduce kernel call cost

```

!$omp parallel do private(...)
!$acc kernels
!$acc loop independent gang
do ip= 1, PEsmptOT
  ip1=(ip-1)*NCOLORtot + ic
!$omp simd
!$acc loop independent vector
do i= index(ip1-1)+1, index(ip1)
  ...
enddo
enddo
!$omp end parallel do
!$acc end kernels
    
```

Baseline Implementation of OpenMP/OpenACC

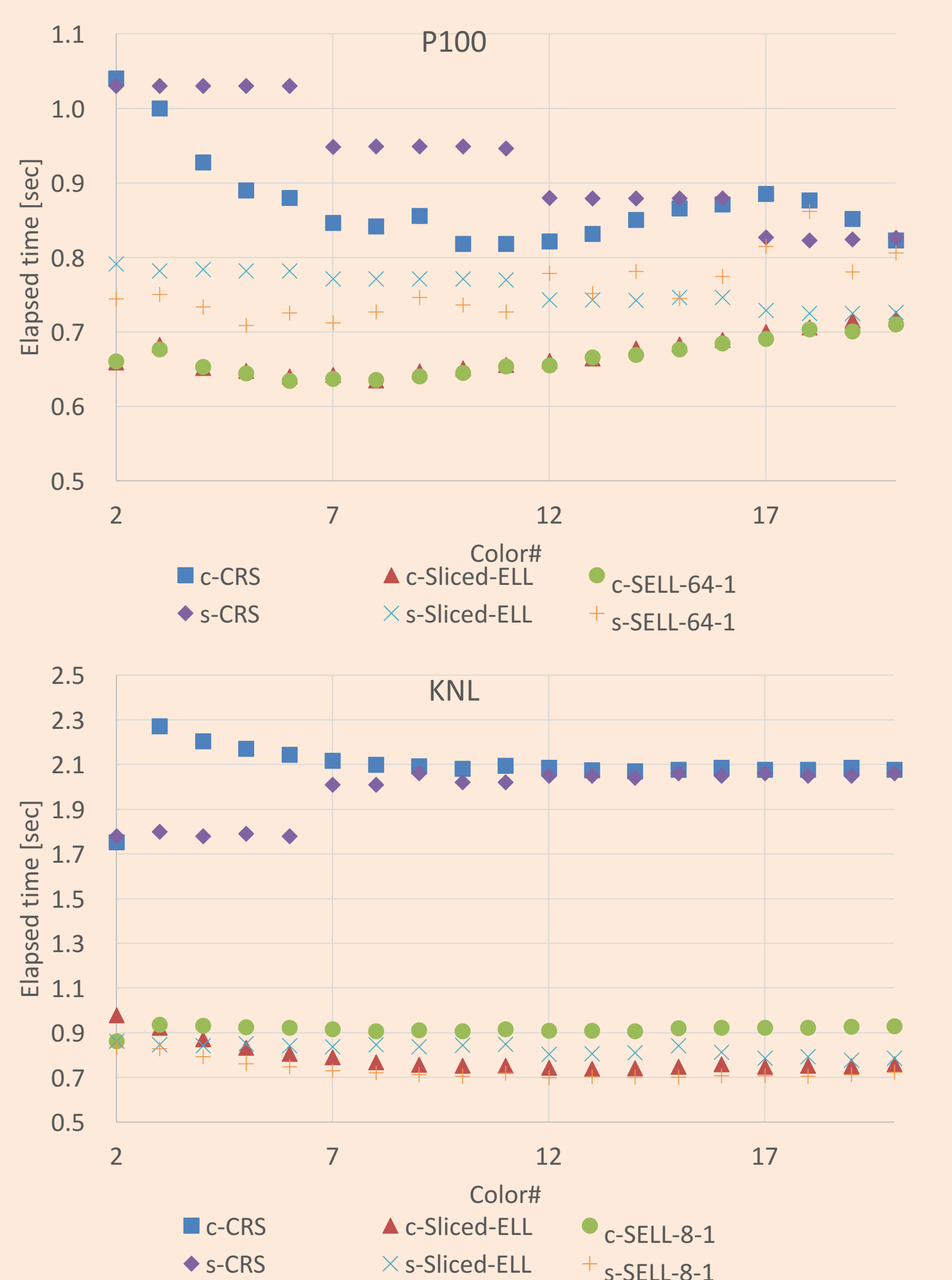
- Optimizations for KNL
  - Baseline
    - ✓ Insert !\$acc parallel do to all loops to be parallelized
  - mvparallel 1
    - ✓ Move !\$acc parallel to outside of color loop
  - nowait
    - ✓ Use !\$omp end do nowait
  - mvparallel 2
    - ✓ Move !\$parallel to outside of convergence loop
  - rmompdo
    - ✓ Parallelize loops by hand without using !\$omp do
  - rmreduction
    - ✓ Reduction by hand
  - loopscheduling
    - ✓ Parallelize loops by using application knowledge

	GPU P100	GPU K20	Xeon Phi KNL	Xeon Phi KNC	Broadwell
Frequency (GHz)	1.480	0.732	1.40	1.053	2.10
Core# (Max thread#)	1,792	896	68 (272)	60 (240)	18 (18)
Peak Performance (GFLOPS)	5,304	1,311	3,046	1,010	604
Memory (GB)	16	6	16	8	128
Bandwidth (GB/sec., Stream Triad)	534	179	490	159	65.5
System	Reedbush-H	TSUBAME2.5	Oakforest-PACS	KNSC	Reedbush-U

Evaluation cases

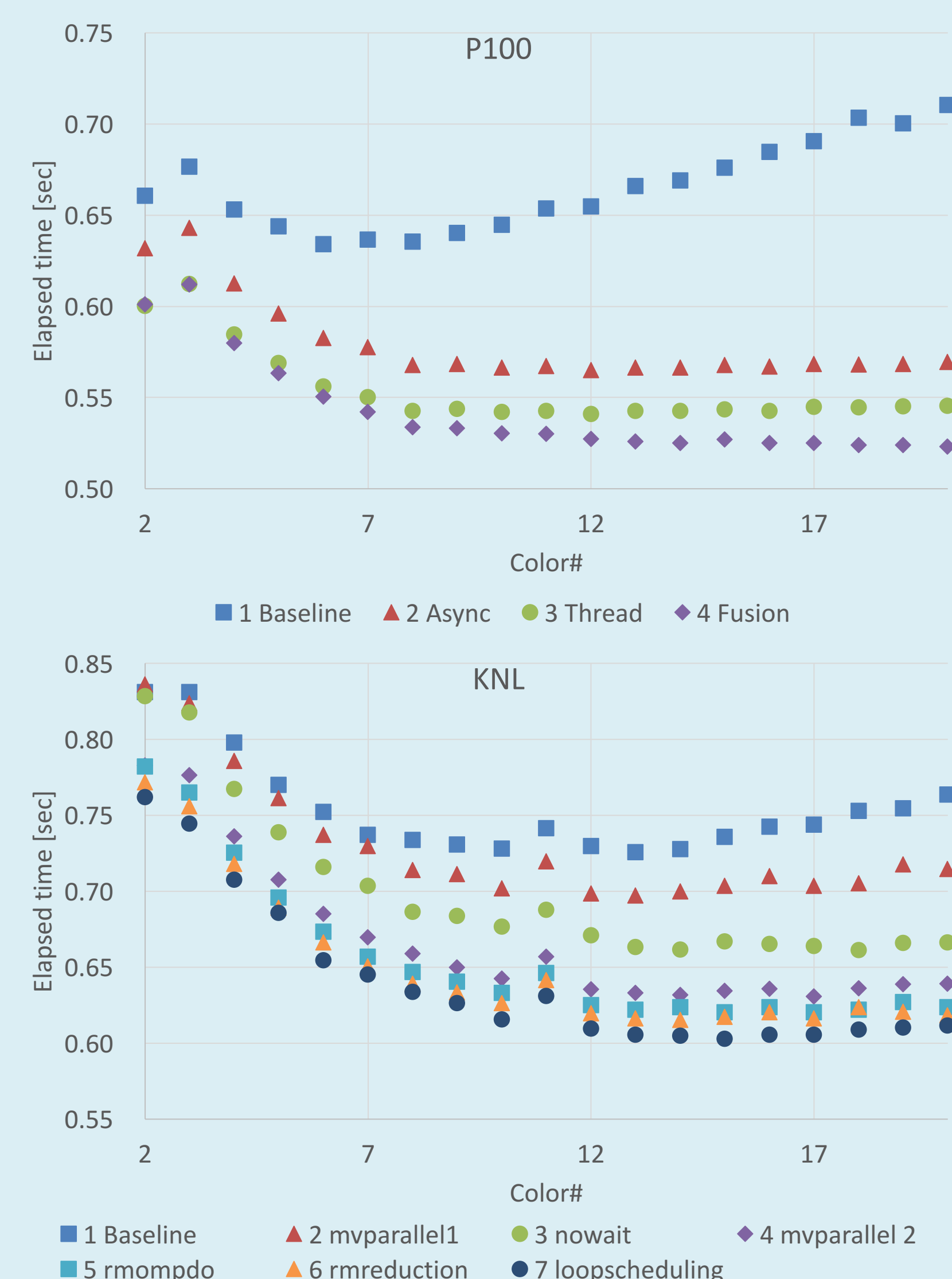
	Numbering	Storage of Matrix
c-CRS	Coalesced	CRS
c-Sliced-ELL		Sliced-ELL (wit blockin)
c-SELL-C- $\sigma$		SELL-C- $\sigma$
s-CRS	Sequential	CRS
s-Sliced-ELL		Sliced-ELL (with blocking)
s-SELL-C- $\sigma$		SELL-C- $\sigma$

### Evaluation of the Numbering and Storage of Matrix (Baseline version)



### Evaluation of the optimizations

- Reducing synchronization costs is important
  - ✓ Attach async clause, which reduces the kernel call overhead, is most effective for P100
  - ✓ A series of optimization, which reduces synchronization, is effective for KNL



### Performance of the baseline version

