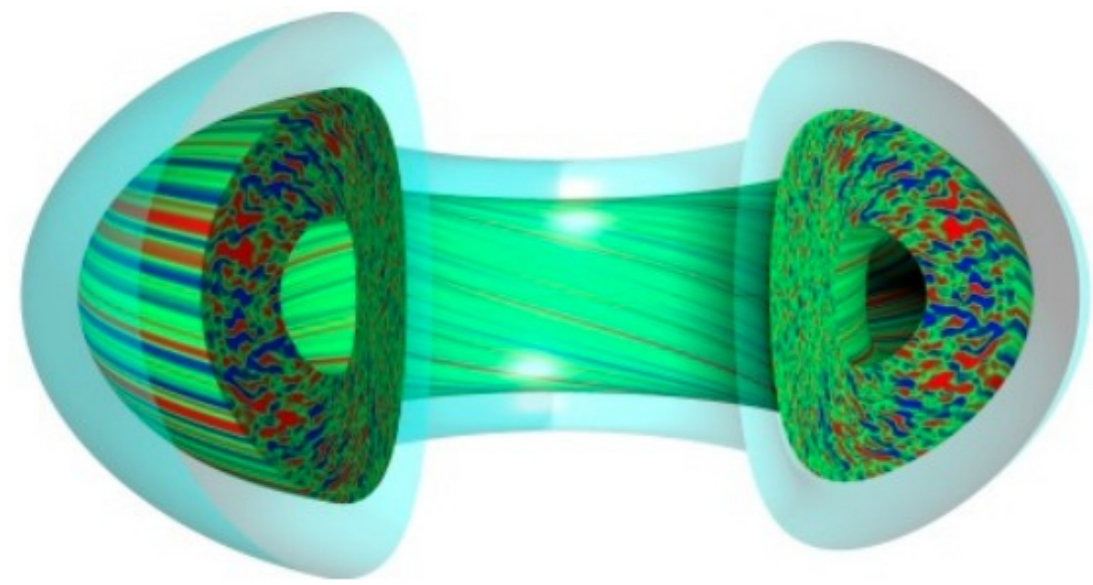


Approach

Solve a higher-dimensional **5(+1)-d** gyrokinetic system for the simulation of fusion plasma microturbulence



$$\frac{\partial F}{\partial t} + \dot{\mathbf{x}} \cdot \nabla F + \dot{v}_{\parallel} \frac{\partial F}{\partial v_{\parallel}} + \mu \frac{\partial F}{\partial \mu} = 0$$

w.r.t. the distribution function $F(x, y, z, v_{\parallel}, \mu, t)$

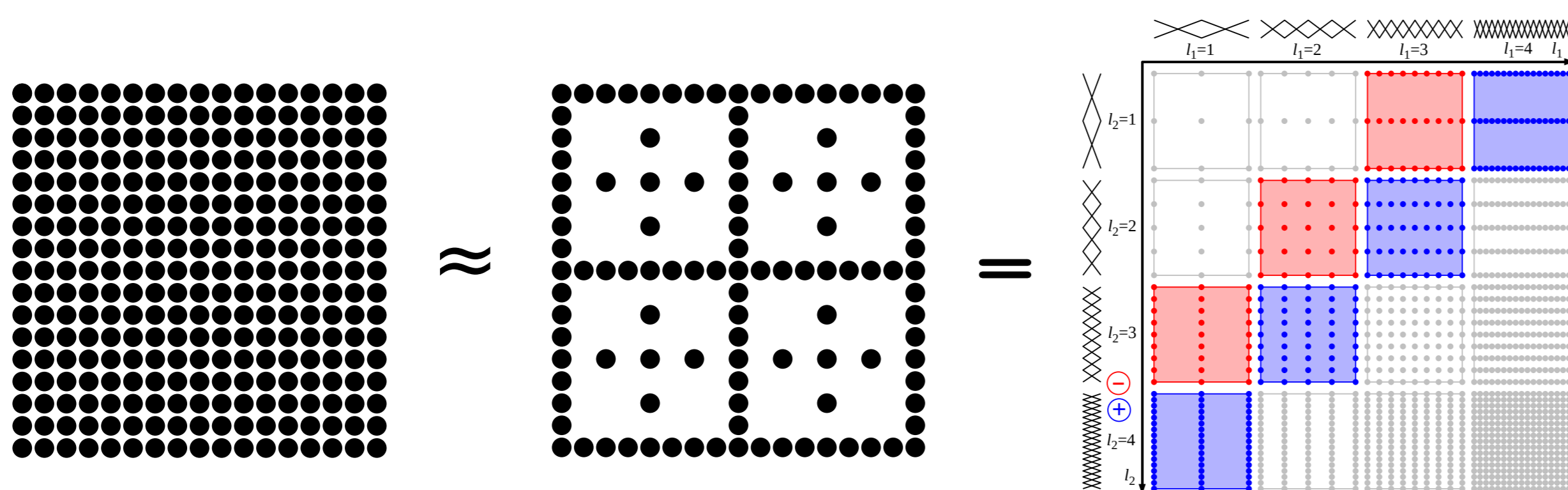
Our aim: to globally solve the gyrokinetic equations for ITER

But: Standard simulations in higher d suffer the **curse of dimensionality**

$$N = \frac{1}{h}, \quad \#points \sim \mathcal{O}(N^d), \quad error \sim \mathcal{O}(N^{-2}) \quad (\text{typically})$$

Sparse Grid Combination Technique to numerically decouple problem: combine partial solutions on regular grids

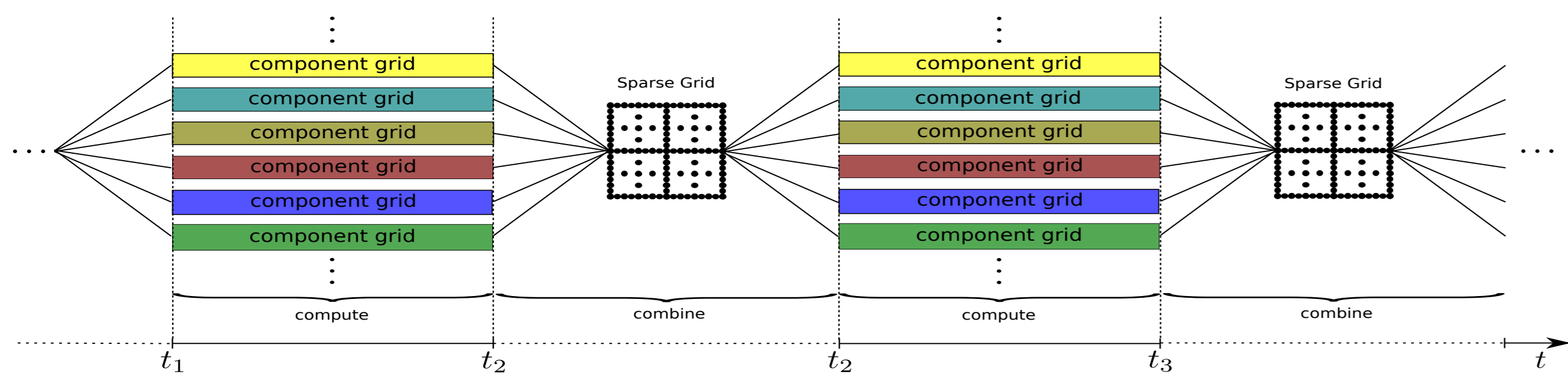
$$\#points \sim \mathcal{O}(d(\log N)^{d-1}) \cdot \mathcal{O}(N), \quad error \sim \mathcal{O}(N^{-2}(\log N)^{d-1})$$



$$u(x) \approx \sum_{q=0}^{d-1} (-1)^q \binom{d-1}{q} \sum_{|I|=n-q} u_I(x)$$

The partial solutions $u_I(x)$ are **independent**

⇒ existing solvers can be used – embarrassingly parallel

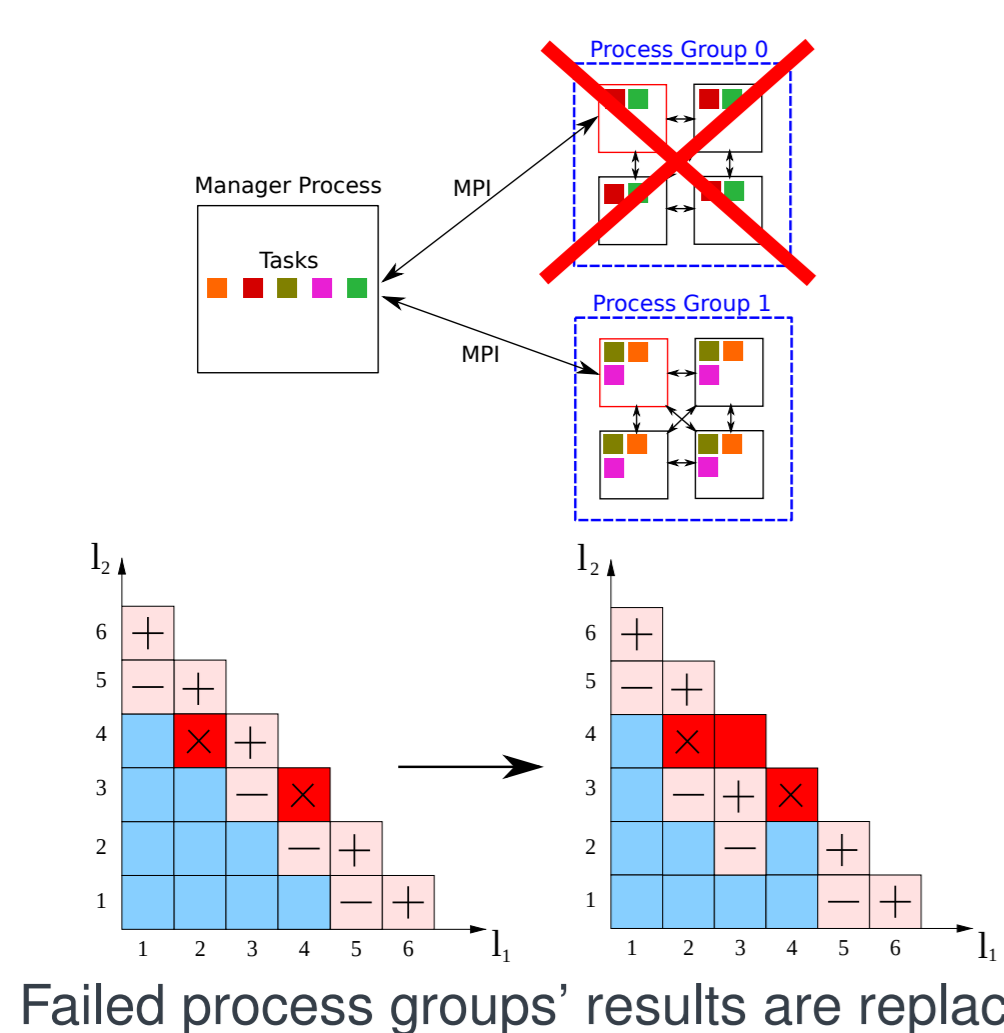


Fault Tolerance

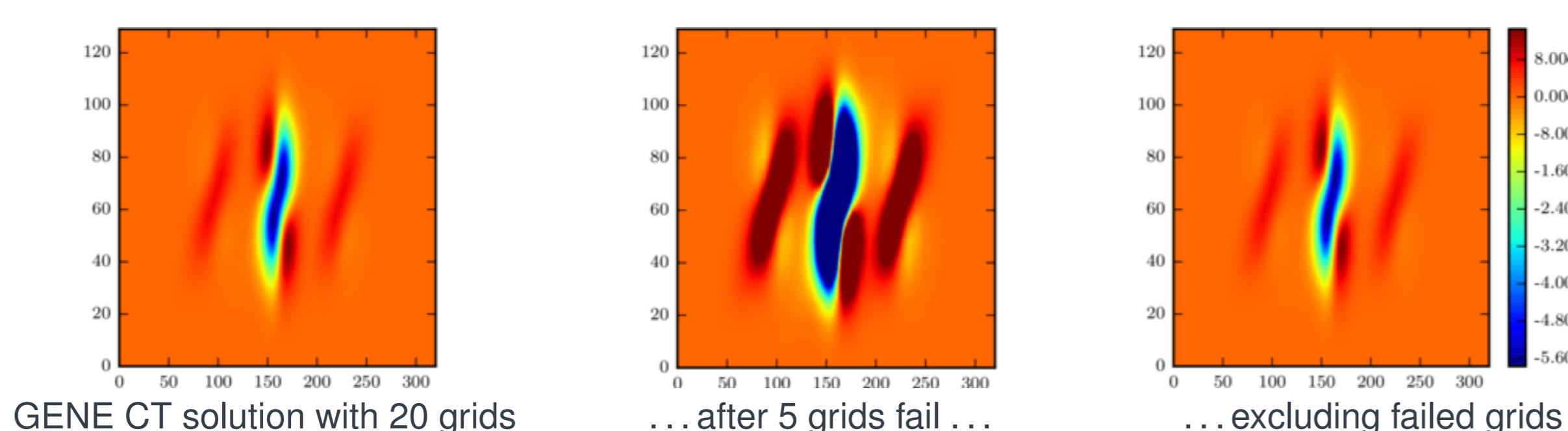
Hardware failures are becoming a problem for exascale.

Fault-Tolerant Combination Technique:

algorithm-based fault tolerance for **hard** and **soft** faults – no checkpoint/restart



```
while not converged
  for all CT grids  $\Omega_l$  do in parallel
     $u_l = \text{solver}(u_l, N_t)$ ; // solve  $N_t$  steps
    decideToKill(); // hard faults
    decideToChange(); // soft faults
    checkForSDC(); // sanity check
    recover(); // mitigate faults
     $u_n^{(c)} = \text{reduce}(c_l u_l)$ ; // combine
    forall  $l \in \mathcal{I}_{n,q}$  do
       $u_l = \text{scatter}(u_n^{(c)})$ ; // re-distribute
```



⇒ **good approximation** even after recovery

The Project

Vision

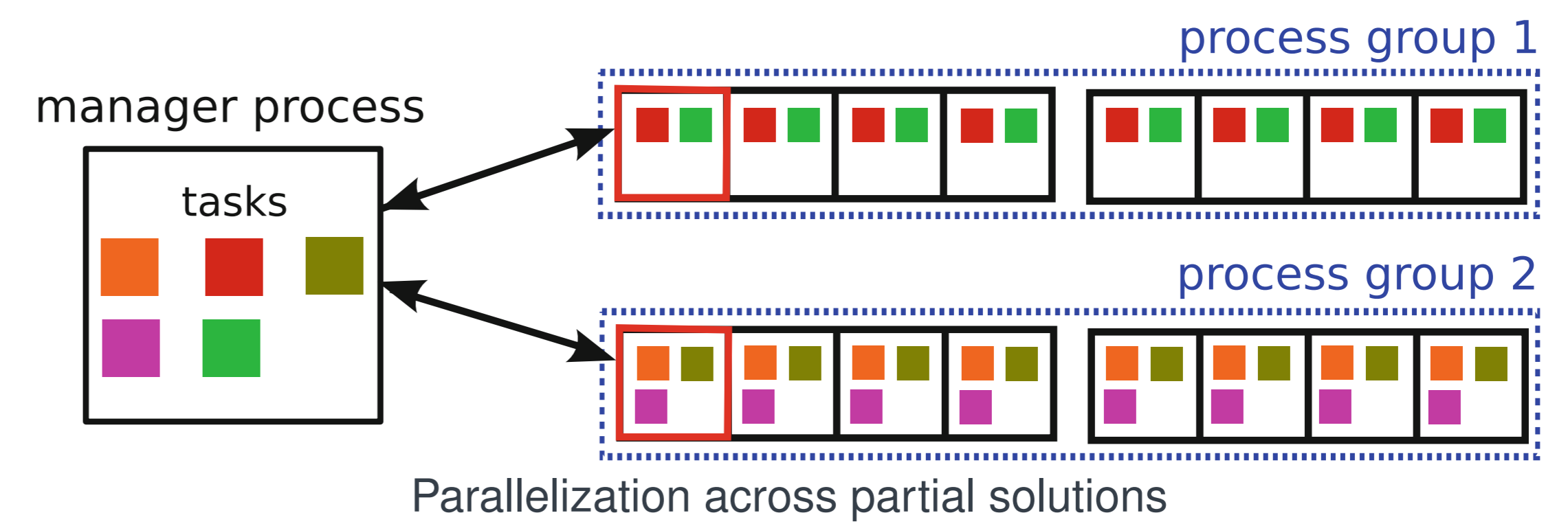
- Algorithms fit to Exascale: Fault tolerance for higher-dimensional problems on all levels of parallelization, and scaling beyond single HPC systems.
- Software Framework: A general tool for the solution of higher-dimensional problems, with efficient adaptive and dynamic load balancing.
- Numerical ITER: Drive GENE code to scenarios that are far beyond what is currently feasible.

Team

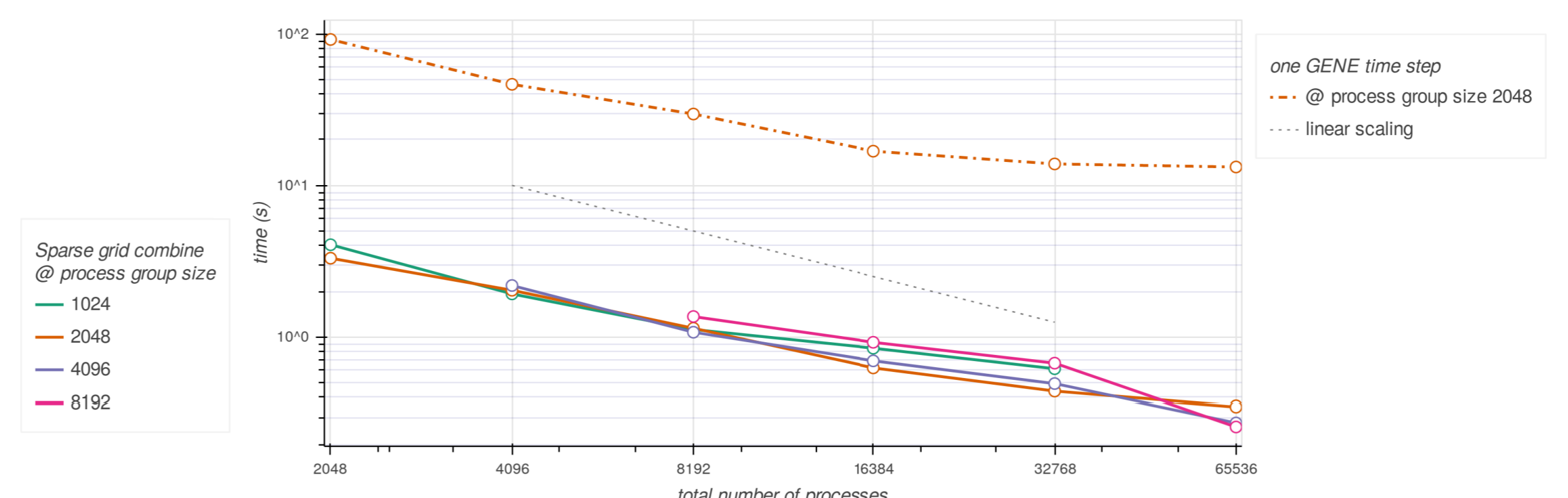


Scaling with an Extra Level of Parallelism

In addition to GENE MPI & OpenMP: **Manager-Worker Pattern**



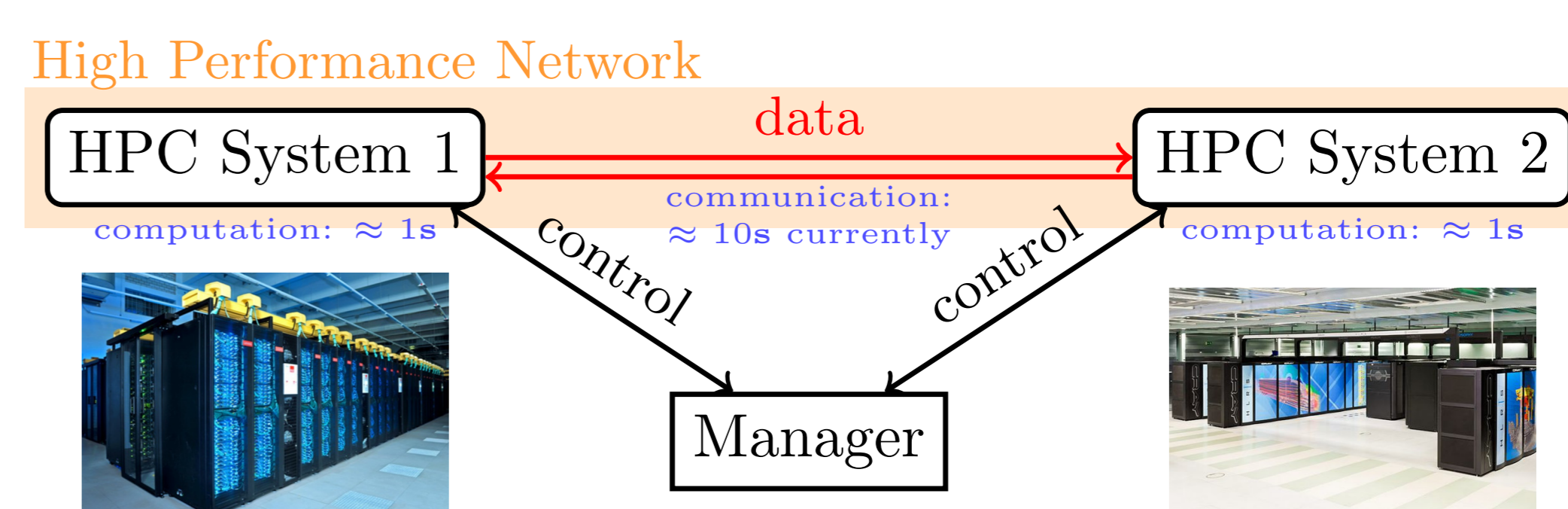
Performance



The combination technique overhead scales at a level negligible to the GENE set-up

WIP: Scaling Beyond Single HPC Systems

As the problem sizes get larger, why not **couple more HPC Systems?**



Publications and More

At ipvs.informatik.uni-stuttgart.de/SGS/EXAHD/

