

# PHYSICAL OSCILLATOR MODEL FOR PARALLEL DISTRIBUTED COMPUTING

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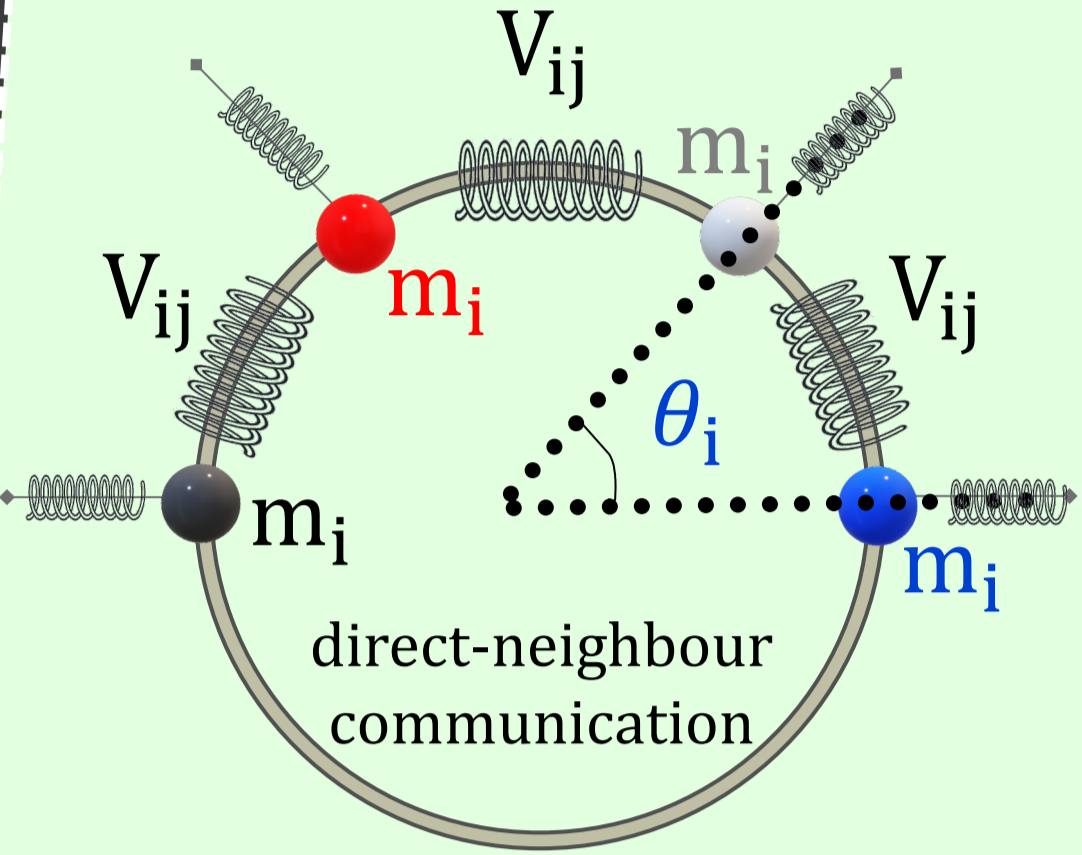
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## MOTIVATION

Analytic, first-principles performance modelling of distributed-memory applications is not available due to a wide spectrum of effects cause by noise and complex interplay between code, message passing library and cluster

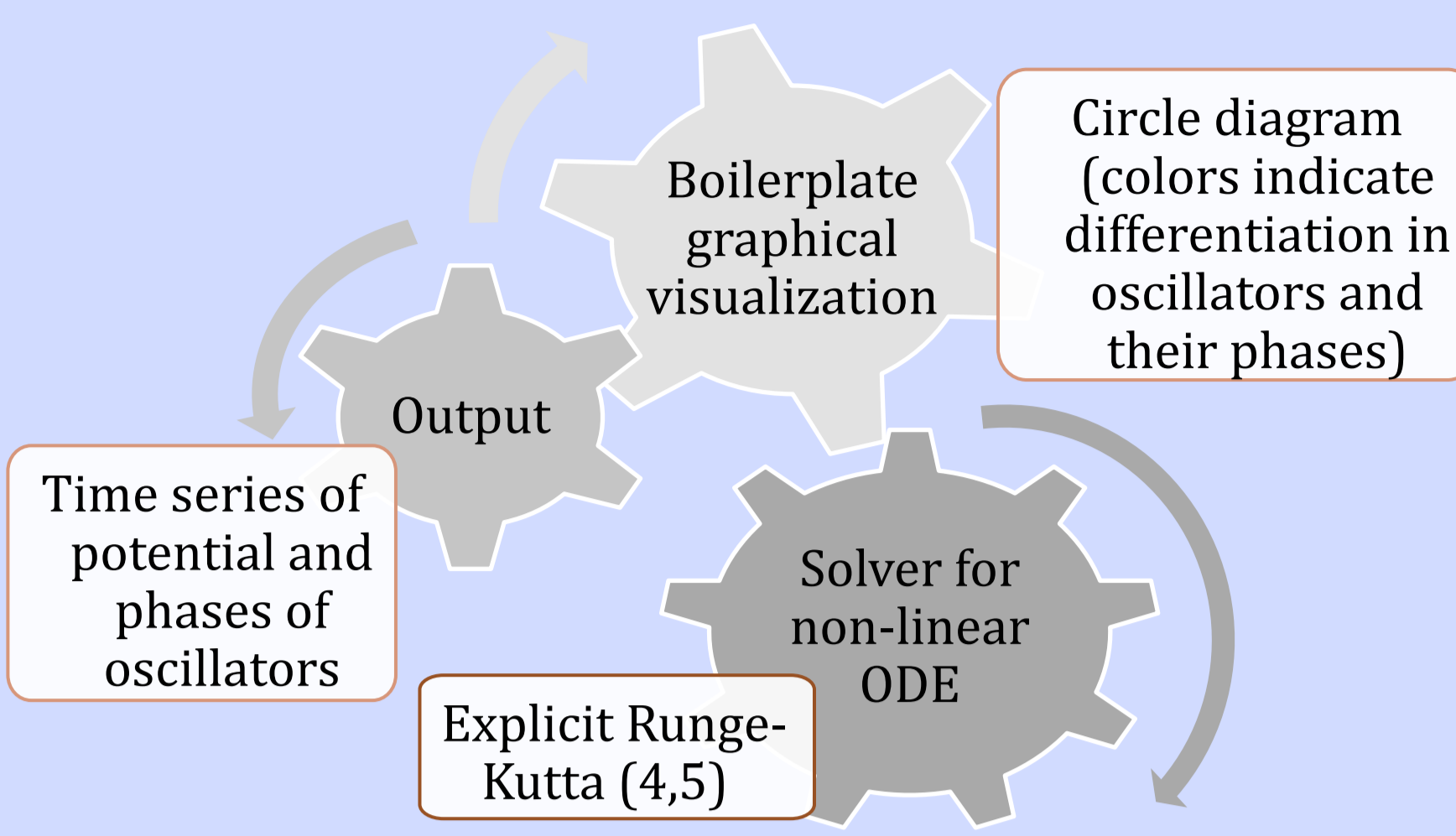
We propose a non-linear physical coupled phase oscillators model

Bridging the gap: a theoretical model for a comprehensive insight of global consequences on performance in (non-)equilibrium states of (ir)regular applications

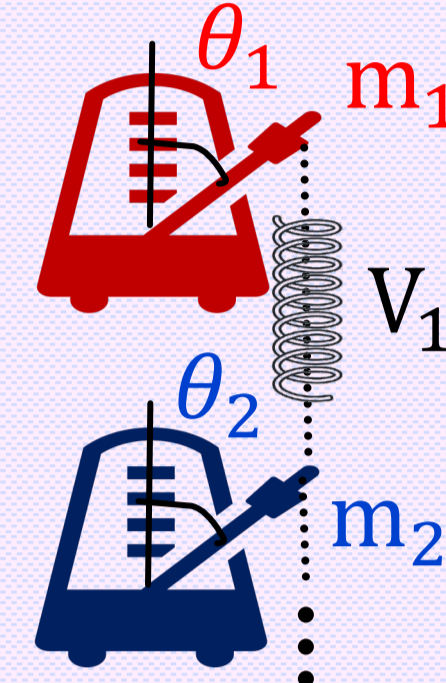


The phenomenology of distributed applications suggests a physical interpretation of individual processes as point masses moving in the potential that accelerates or slows down the oscillation

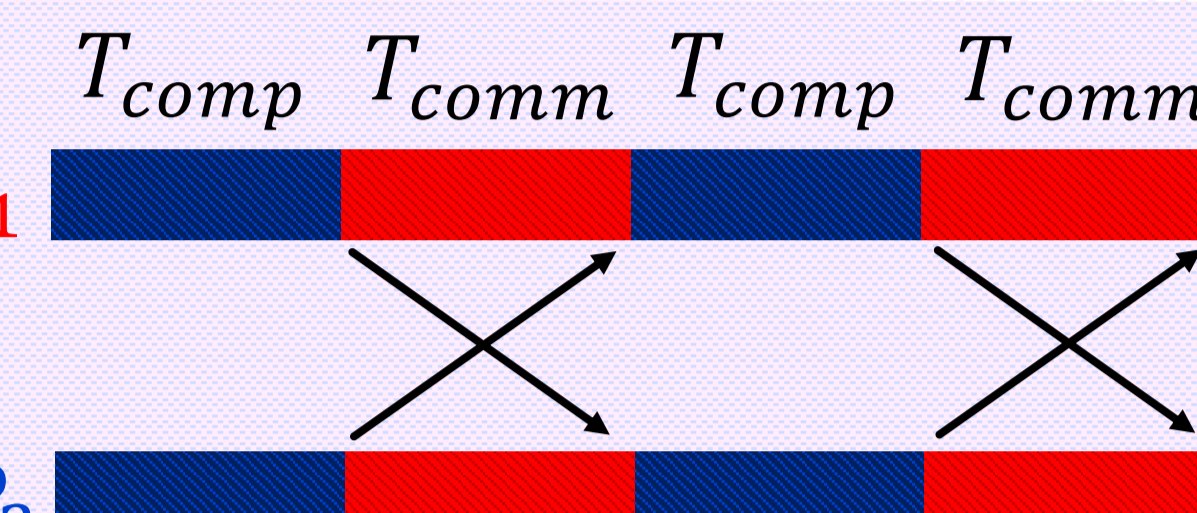
## MODEL IMPLEMENTATION



simple and cheap experiments  
solving a system of first-order coupled ODEs



analogy unknown in parallel computing



running highly parallel programs on supercomputers

## ANALOGY COMPARISON

Parallel Programs	Physical Model
number of processes $Comm\_size$	number of oscillators $N$
alternate back-and-forth $1/(T_{comp} + T_{comm})$	intrinsic natural frequency $\omega_i$
variability in $T_{comp}$ and $T_{comm}$ of processes	phase differences (noise) or frequencies spread (load imbalance) of oscillators
delay propagation speed (the distance in ranks travelled in one time step)	coupling strength $K$

$$\dot{\theta}_i = \omega_i + \zeta_i(t) + \frac{\sigma \cdot K}{sum(T_{exec}, T_{comm}) \cdot comm\_size} \sum_{j=1}^N T_{ij} V_{ij}(\theta(t, \tau))$$

$comm\_size$ : system size  
 $T_{exec}, T_{comm}$ : execution time, communication time  
 $\sigma, \kappa$  and  $T_{ij}$  (dimensionless): depend on the communication protocol, concurrency, and topology  
 $V_{ij}(\theta)$ : coupling potential reflects bottleneck structure  
 $\zeta_i(t)$ : local noise;  $\tau$ : interaction noise

## MODEL COMPARISON

Kuramoto Model vs Coupled Oscillator Model

$$\dot{\theta}_i = \omega_i + \frac{K}{N} \sum_{j=1}^N \sin(\theta_j - \theta_i)$$

- |  |                       |   |
|--|-----------------------|---|
| <input type="checkbox"/> global full-connectivity  | $\longleftrightarrow$ | topology-aware pairwise local interactions                              |
| <input type="checkbox"/> no delay propagation over timestep                                      | $\longleftrightarrow$ | delay propagation over timestep   |
| <input type="checkbox"/> period of an oscillator (one revolution) = $2\pi$                       | $\longleftrightarrow$ | period of a process (one timestep) = $T_{comm} + T_{comp}$              |
| <input type="checkbox"/> too continuous Ansatz causing built-in noise                            | $\longleftrightarrow$ | discrete Ansatz   |
| <input type="checkbox"/> equilibrium state and its stability is governed by sinusoidal potential | $\longleftrightarrow$ | equilibrium state and its stability is governed by bottleneck structure |

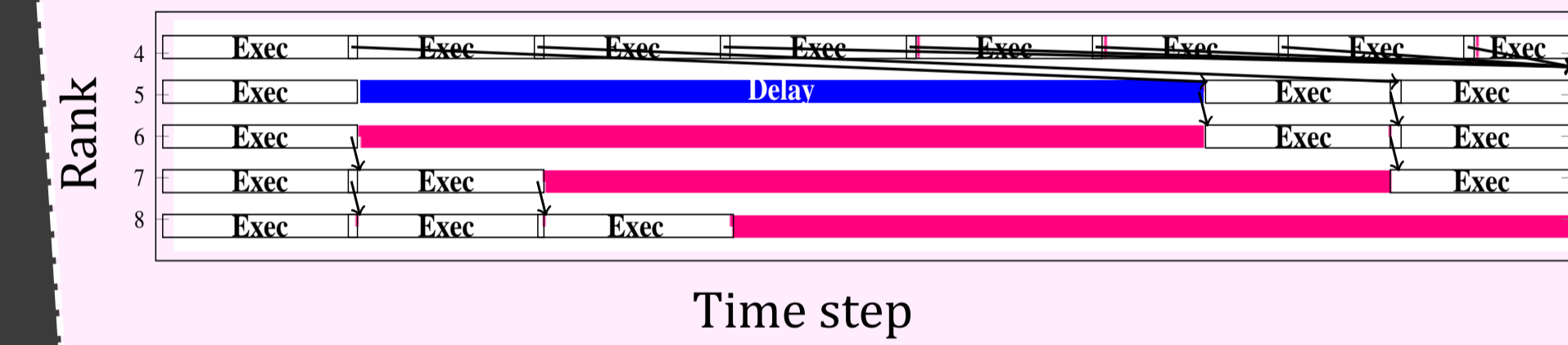
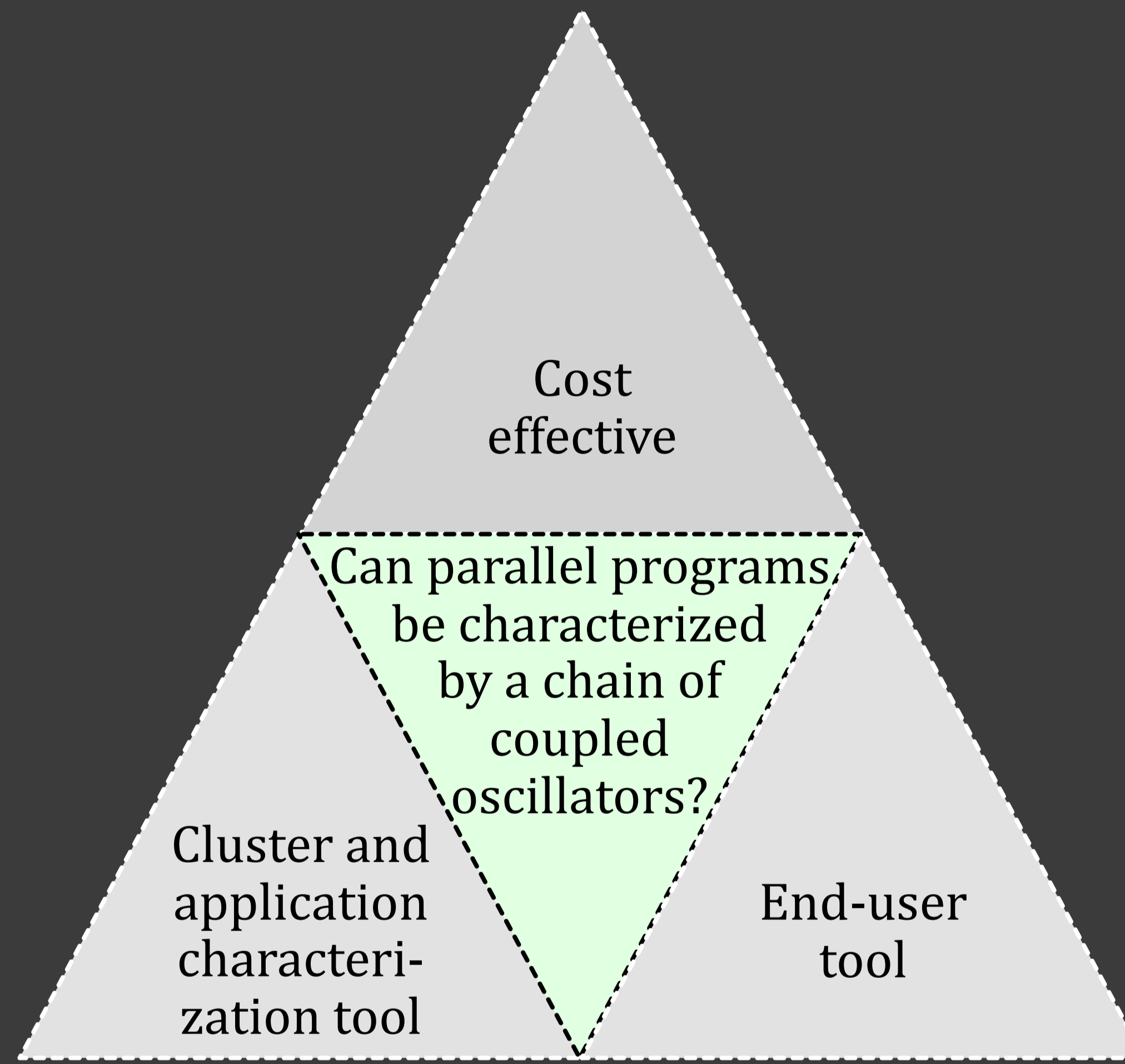
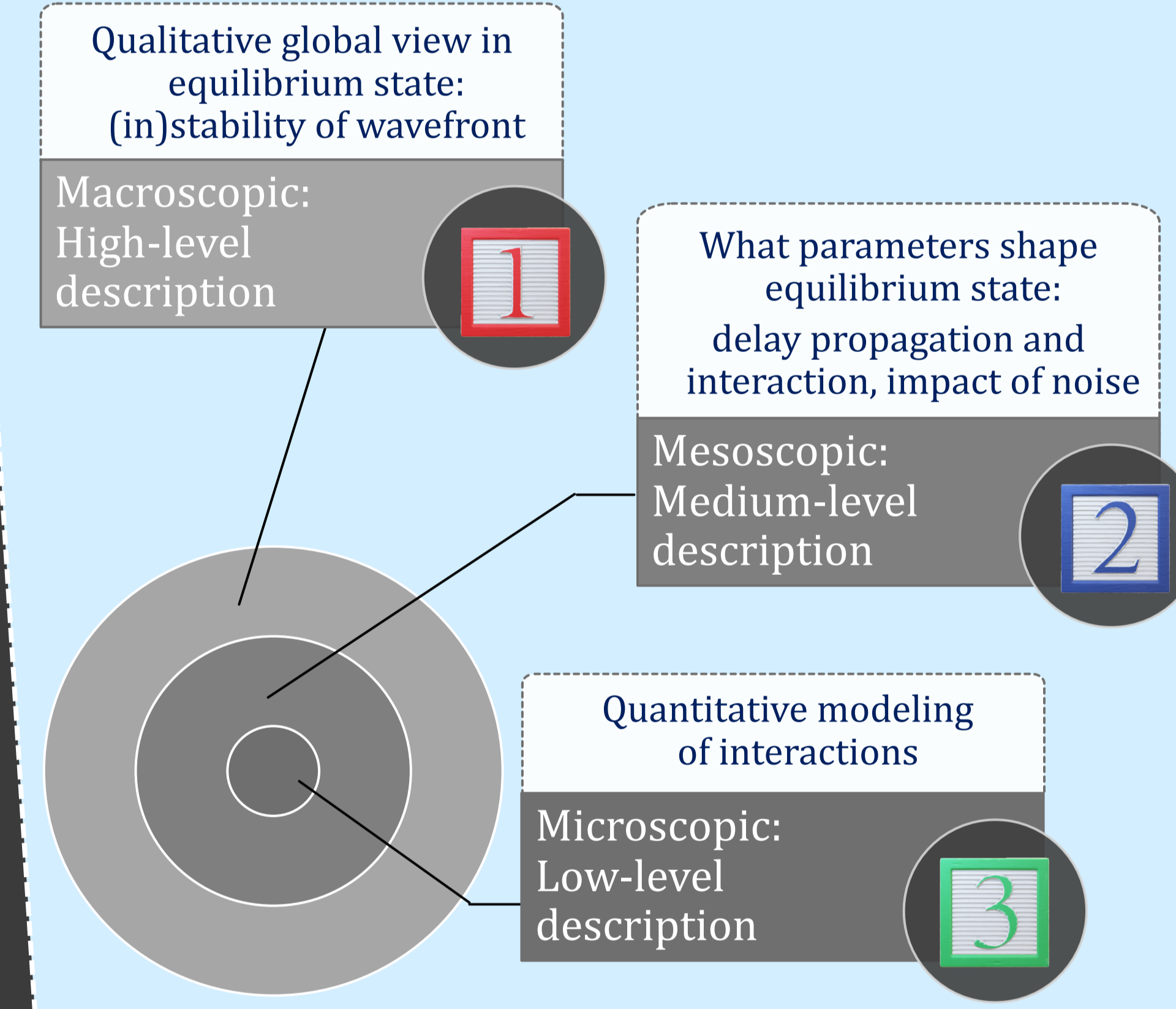


Fig: Delay propagation in MPI parallel programs

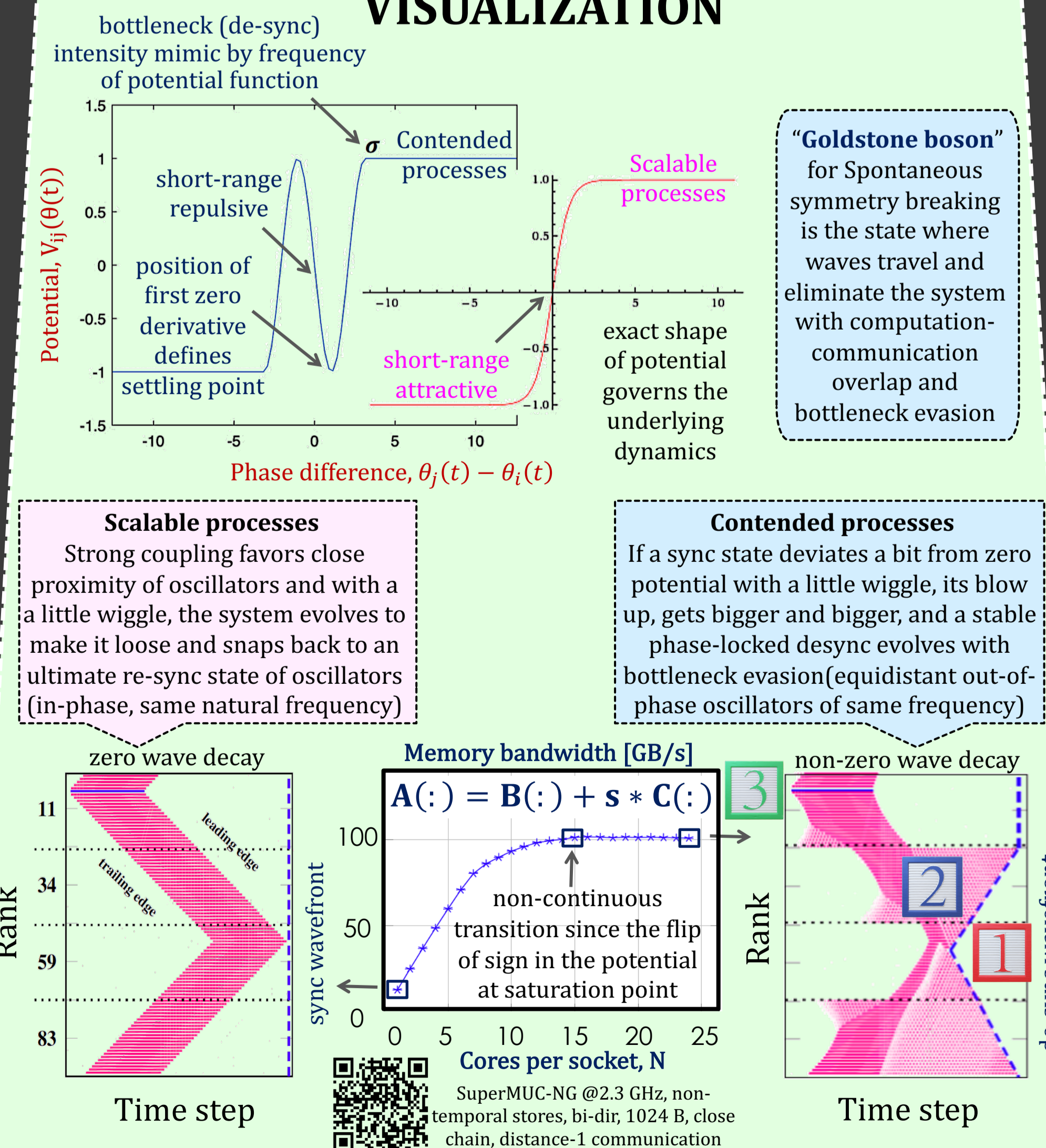
## USEABILITY AND GENERIZATION



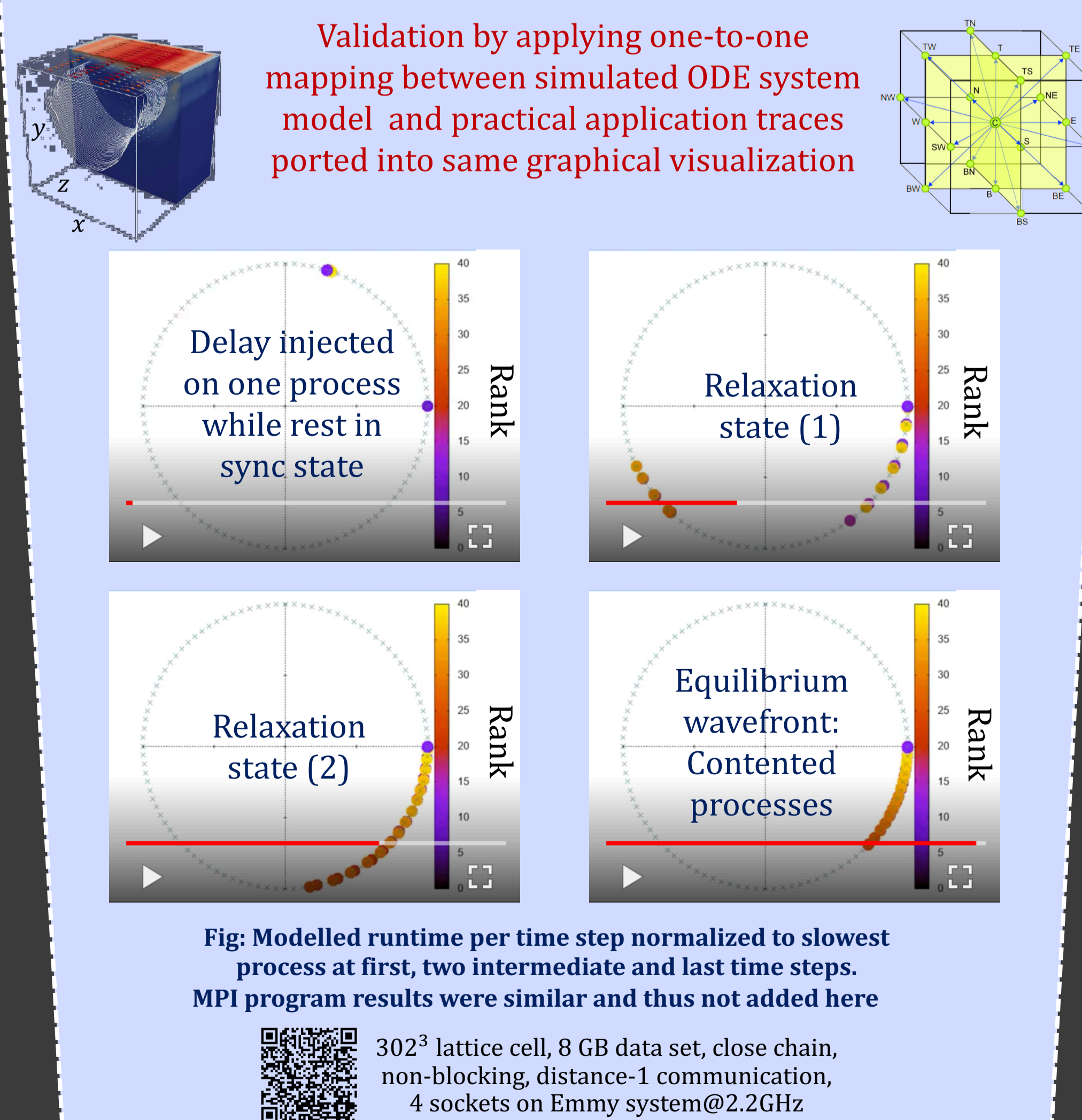
## MODEL APPLICABILITY



## POTENTIAL VS. SCALABILITY VISUALIZATION



## MODELLING EVALUATION USE CASE: LATTICE BOLTZMANN FLUID SOLVER



## OUTLOOK CONCLUSIONS AND LIMITATIONS

- Our model is a novelty and opens possibilities for future research in new directions
- Works at macroscopic (1) and mesoscopic (2) levels
- Limitations at microscopic (3) level since non-differentiable nature of the compute-communicate oscillation
- Model Modification for best interaction term for accuracy and further useability is intended as future work

Afzal et al. [QR codes and DOIs]

